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# Superior energy density through tailored dopant strategies in multilayer ceramic capacitors†

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The Gerson–Marshall (1959) relationship predicts an increase in dielectric breakdown strength (BDS) and therefore, recoverable energy density ( $W_{\text{rec}}$ ) with decreasing dielectric layer thickness. This relationship only operates however, if the total resistivity of the dielectric is sufficiently high and the electrical micro-structure is homogeneous (no short circuit diffusion paths). BiFeO<sub>3</sub>–SrTiO<sub>3</sub> (BF–ST) is a promising base for developing high energy density capacitors but Bi-rich compositions which have the highest polarisability per unit volume are ferroelectric rather than relaxor and are electrically too conductive. Here, we present a systematic strategy to optimise BDS and maximum polarisation *via*: (i) Nb-doping to increase resistivity by eliminating hole conduction and promoting electrical homogeneity and (ii) alloying with a third perovskite end-member, BiMg<sub>2/3</sub>Nb<sub>1/3</sub>O<sub>3</sub> (BMN), to reduce long range polar coupling without decreasing the average ionic polarisability. These strategies result in an increase in BDS to give  $W_{\text{rec}} = 8.2 \text{ J cm}^{-3}$  at  $460 \text{ kV cm}^{-1}$  for BF–ST–0.03Nb–0.1BMN ceramics, which when incorporated in a multilayer capacitor with dielectric layers of  $8 \mu\text{m}$  thickness gives  $\text{BDS} > 1000 \text{ kV cm}^{-1}$  and  $W_{\text{rec}} = 15.8 \text{ J cm}^{-3}$ .

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### Broader context

Successful decarbonisation of the world economy will be underpinned by efficient energy harvesting and storage technologies. Batteries exhibit high energy density but low power density, making them unsuitable for applications requiring fast charge–discharge rates. In contrast, dielectric capacitors widely used in pulsed power electronics have intrinsically higher power density. The next generation of dielectric capacitors for energy storage applications will be required to have higher energy density, discharge efficiency, and breakdown strength for higher voltage applications. In addition, finding less toxic, lead-free materials has been a major scientific and technological challenge. Here, we demonstrate tailored dopant strategies in lead-free BiFeO<sub>3</sub>–SrTiO<sub>3</sub> (BF–ST) based energy storage capacitors to increase resistivity, promote electrical homogeneity and reduce polar coupling without decreasing the average ionic polarisability. By employing both strategies, a record high energy density in BF–ST is attained in multilayer ceramic capacitors. This work sheds new light on designing ultrahigh energy storage materials and can be employed in most high polarisability oxide-based materials.

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## 1. Introduction

As world economies grow and are required to decarbonise, the increasing demand for more efficient energy storage and utilisation has led to worldwide interest in the development of capacitors.<sup>1,2</sup> Dielectric capacitors have attracted attention for advanced pulsed power applications due to their high power densities and fast charge–discharge rates in contrast to batteries which have high energy but low power densities.<sup>3–5</sup> Currently however, the low energy storage densities compared to batteries limits their applications.<sup>6–9</sup> Most commercial dielectric capacitors are utilised as decouplers and filters in consumer electronics which require energy density  $< 1 \text{ J cm}^{-3}$ , too low for near-engine power electronics in electric vehicles and ‘down-hole’



pulsed power applications which require high voltage, temperature and power density.<sup>10</sup>

The recoverable energy storage density of dielectric capacitors ( $W_{\text{rec}}$ ) can be obtained using the following equation:

$$W_{\text{rec}} = \int_{P_r}^{P_{\text{max}}} E dP, \quad (1)$$

where  $P_{\text{max}}$  and  $P_r$  are the maximum polarisation and the remanent polarisation under an applied electric field ( $E$ ), respectively. Typically, high  $W_{\text{rec}}$  is achieved by a combination of large  $P_{\text{max}}$ , small  $P_r$  and high dielectric breakdown strength (BDS). However, high permittivity ( $\epsilon_r$ ) dielectrics with large  $P_{\text{max}}$  generally exhibit relatively high dielectric loss, resulting in low BDS and  $W_{\text{rec}}$ .<sup>11</sup> Approaches based on tailoring extrinsic properties to improve BDS include decreasing dielectric layer thickness,<sup>12,13</sup> reducing porosity,<sup>14,15</sup> decreasing grain size<sup>16,17</sup> and potentially introducing a core-shell grain structure.<sup>18,19</sup> Tailoring of intrinsic properties include increasing the band gap,<sup>20</sup> promoting electrical homogeneity,<sup>21</sup> and decreasing the total conductivity. The importance of the band gap on BDS has been studied<sup>20</sup> and electrical homogeneity has proved to be an effective way to improve BDS and enhance  $W_{\text{rec}}$ .<sup>21</sup> However, there are few studies which detail a systematic approach on the influence of electrical conductivity in optimising  $W_{\text{rec}}$ .

In general, conductivity  $\sigma$  is given by:

$$\sigma = nq\mu, \quad (2)$$

where  $n$  is the carrier concentration,  $q$  is the charge of charge carrier and  $\mu$  is the mobility of the charge carrier. For dielectric ceramics,  $n$  plays a pivotal role in controlling  $\sigma$ . This is normally achieved by optimising processing conditions (*e.g.* sintering atmosphere/temperature, cooling rates) and/or through the use of aliovalent dopants.

Aliovalent doping has long been an effective way to tailor the electrical performance of oxides. Acceptor (*e.g.*  $\text{Ca}^{2+}$  for  $\text{Ti}^{4+}$ ) doping in  $\text{BaTiO}_3$  facilitates the formation of oxygen vacancies, prevents the reduction of  $\text{Ti}^{4+}$  when sintered in low oxygen partial pressure atmospheres and therefore, reduces leakage current.<sup>22,23</sup> In contrast, donor doping  $\text{BaTiO}_3$  (*e.g.*  $\text{La}^{3+}$  for  $\text{Ba}^{2+}$ ) creates metal (Ti) vacancies that result in the loss of oxygen ( $\delta$ ) from the lattice when sintering in air above 1300 °C:  $\text{Ba}_{1-x}\text{La}_x\text{Ti}_{1-x/4}\text{O}_{3-\delta}$  ceramics are n-type semiconducting for low levels of  $x$ .<sup>24,25</sup> In some cases, there can be significant levels of oxide-ion conductivity such that, ionic as opposed to electronic conduction, dominates the electrical properties. For example, oxygen vacancies can occur in  $\text{Na}_{1/2}\text{Bi}_{1/2}\text{TiO}_3$  (NBT) due to acceptor doping and/or  $\text{Bi}_2\text{O}_3$ -loss during processing and leads to high levels of oxide-ion conductivity.<sup>26,27</sup> Donor doping with low levels of  $\text{Nb}^{5+}$  for  $\text{Ti}^{4+}$  *via* the mechanism in eqn (3) is an effective method to compensate for the formation of oxygen vacancies during processing and suppresses ionic conductivity such that dielectric behavior is restored.<sup>26</sup>



The choice of dopants to enhance or suppress  $n$  requires an understanding of the defect chemistry, the possible charge

carrier type(s) and plausible conduction mechanism(s) for each particular material.

$\text{BiFeO}_3$  (BF)-based ceramics are a promising 'next generation' of lead-free electroceramics for applications as high energy density capacitors, piezoelectrics, ferroelectrics, electrocalorics and multiferroics.<sup>28–38</sup> However, the low BDS (high leakage current), resulting from the volatilisation of  $\text{Bi}_2\text{O}_3$  and consequent oxidation of some  $\text{Fe}^{3+}$  to  $\text{Fe}^{4+}$  ions is one of the main obstacles to their commercial usage.<sup>39,40</sup> In this work,  $\text{BiFeO}_3$ - $\text{SrTiO}_3$  (BF-ST)-based ceramics are used as a case study to illustrate how materials can be systematically modified to create exceptional dielectric properties suitable for electroceramic applications.

0.4BF–0.6ST has been previously proposed as a novel and high temperature lead-free ceramic achieving high energy density of  $W_{\text{rec}} = 6.0 \text{ J cm}^{-3}$  at  $420 \text{ kV cm}^{-1}$  in multilayer ceramic capacitors (MLCCs).<sup>41</sup> We propose that BF-rich compositions, which were not reported by the authors of ref. 41, could potentially exhibit higher energy density due to their higher ionic polarisability per unit volume which leads to the appearance of spontaneous polarisation. BF-rich compositions are typically p-type semiconductors<sup>39</sup> and too leaky for high energy density capacitor applications. Moreover, they are predominantly ferroelectric rather than relaxor and hence in their initial state have intrinsically low  $W_{\text{rec}}$ .<sup>42</sup> A systematic study was therefore undertaken of 0.6BF–0.4ST (reported as a nominal morphotropic phase boundary, MPB, composition)<sup>43</sup> using (i) doping with Nb on the B-site to control  $\sigma$  and induce electrical homogeneity and (ii) alloying with a third end-member,  $\text{BiMg}_{2/3}\text{Nb}_{1/3}\text{O}_3$  (BMN) to promote a relaxor state without decreasing the average ionic polarisability. Record-high  $W_{\text{rec}}$  of 8.2 and  $15.8 \text{ J cm}^{-3}$  for lead-free materials were achieved in 0.5BF–0.4ST–0.03Nb–0.1BMN bulk ceramics and multilayer capacitors, respectively. This work, therefore, defines clear engineering guidelines for designing ultrahigh energy storage materials and can readily be adapted for most high polarisability oxide-based systems.

## 2. Results and discussions

A nominal MPB region is reported in the  $x\text{BF}-(1-x)\text{ST}$  solid solution at  $x \sim 0.6$ .<sup>43</sup> Typically, at an MPB, functional properties such as piezoelectricity,  $\epsilon_r$  and  $P_r$  are enhanced.<sup>31,32</sup> We have therefore, chosen  $x = 0.6$  as the base material for our studies. However, BF-rich compositions typically exhibit a high p-type<sup>39</sup> leakage current with direct evidence of hole conduction through Seebeck measurements as later presented in Section 2.3. Here, in Section 2.1, we describe how donor doping with Nb on the B-site decreases conductivity in compositions with  $x = 0.6$  so that BDS may be enhanced. Sections 2.3 and 2.4 illustrate how Nb doping combined with alloying with a third perovskite end-member, BMN, was employed to produce exceptional dielectric materials with ultrahigh energy densities in MLCCs.

### 2.1. The role of Nb doping

The loss of  $\text{Bi}_2\text{O}_3$  in BF-ST during ceramic processing creates oxygen vacancies at high temperature. Cooling in air from the



sintering temperature leads to ceramic re-oxidation, *i.e.* ceramic grains oxidise to partially fill the oxygen vacancies. To maintain charge neutrality, some  $\text{Fe}^{3+}$  ions are oxidised to  $\text{Fe}^{4+}$  ions and leads to p-type leakage current, with an activation energy ( $E_a$ ) for conduction of  $\sim 0.4$  eV.<sup>44,45</sup> Leakage conductivity is suppressed by inhibiting oxidation (gain of oxygen) on cooling which is achieved by either processing in an inert atmosphere, such as  $\text{N}_2$  or Ar, or by Nb-donor doping according to eqn (3).

Impedance spectroscopy data for 0.6BF–0.4ST ceramics with 0, 1 and 3% Nb are shown in Fig. 1. A  $Z^*$  plot for 0.6BF–0.4ST ceramic (Fig. 1a) exhibits a distorted and broadened arc response at room temperature (RT), with a total resistivity of  $\sim 180$  k $\Omega$  cm. This is consistent with 0.6BF–0.4ST ceramics being leaky dielectrics at RT. The corresponding  $Z''$  and  $M''$  spectroscopic plots (Fig. 1b) show clear evidence of large Debye peaks with the corresponding frequencies for  $Z''$  and  $M''$  maximum,  $f_{\text{max}}$ , separated by  $\sim 2$  orders of magnitude (Fig. 1b). The data are analysed using an equivalent circuit based on two parallel resistor–capacitor (RC) elements connected in series.  $R$  and  $C$  values are extracted from the  $Z''$  and  $M''$  spectra as described previously.<sup>11</sup> The extracted  $C$  values are  $\sim 1 \times 10^{-10}$  F cm $^{-1}$  (based on  $M''$  data, component 2) and  $\sim 4.5 \times 10^{-10}$  F cm $^{-1}$  (based on  $Z''$  data, component 1) which indicates they are bulk (grain) and grain boundary responses, respectively.<sup>46</sup> The full width half maximum (FWHM) of the  $Z''$  and  $M''$  peaks exceeds 2 orders of magnitude in the frequency spectrum suggesting there is considerable electrical heterogeneity associated with 0.6BF–0.4ST ceramics.<sup>32</sup>

For 1 and 3% Nb doped 0.6BF–0.4ST, ceramics are too resistive to measure by impedance spectroscopy at RT and higher temperatures are required to obtain useful data. The  $Z^*$  plots and  $Z''$ ,  $M''$  spectra for these samples at 703 K are shown in Fig. 1c–e. The most obvious difference in the data is the presence of a single arc in the  $Z^*$  data, Fig. 1c and a single  $Z''$  and  $M''$  Debye peak that occurs at the same frequency, Fig. 1d and e. The FWHM of these peaks are  $\sim 1.2$  orders of magnitude, closer to the 1.14 decades for an ideal Debye response. The data are analysed using a single parallel RC element associated with a bulk response and clearly shows that 1–3% Nb doping produces a dramatic increase in electrical resistivity and improves the electrical homogeneity of the ceramics. An Arrhenius plot of the bulk conductivity (extracted from  $M''$  spectra) for all ceramics in this series is given in Fig. 1f and shows that Nb doped ceramics are excellent dielectrics with bulk conductivity  $< 25$   $\mu\text{S cm}^{-1}$  at 703 K in contrast to undoped ceramics with a bulk conductivity that exceed 1  $\mu\text{S cm}^{-1}$  at RT. In addition to the decrease in conductivity, there is a dramatic increase in the  $E_a$  associated with the bulk conductivity from  $\sim 0.37$  to  $\sim 1.18$  eV. This clearly indicates a change in the mechanism.  $\sim 0.4$  eV is consistent with p-type electronic conduction reported in undoped BF and suggests the presence of mixed oxidation states of  $\text{Fe}^{3+}$  and  $\text{Fe}^{4+}$  ions.<sup>45</sup> The band gap of BF is reported to be  $\sim 2.09$  to  $2.32$  eV whereas for ST it is  $\sim 3.2$  eV.<sup>47,48</sup> Although the exact band gap of BF–ST in this study is unknown, based on the end-members, an  $E_a$  of  $\sim 1.2$  eV is reasonably close to half the optical band gap, suggesting that the electronic conduction for the Nb-containing ceramics is

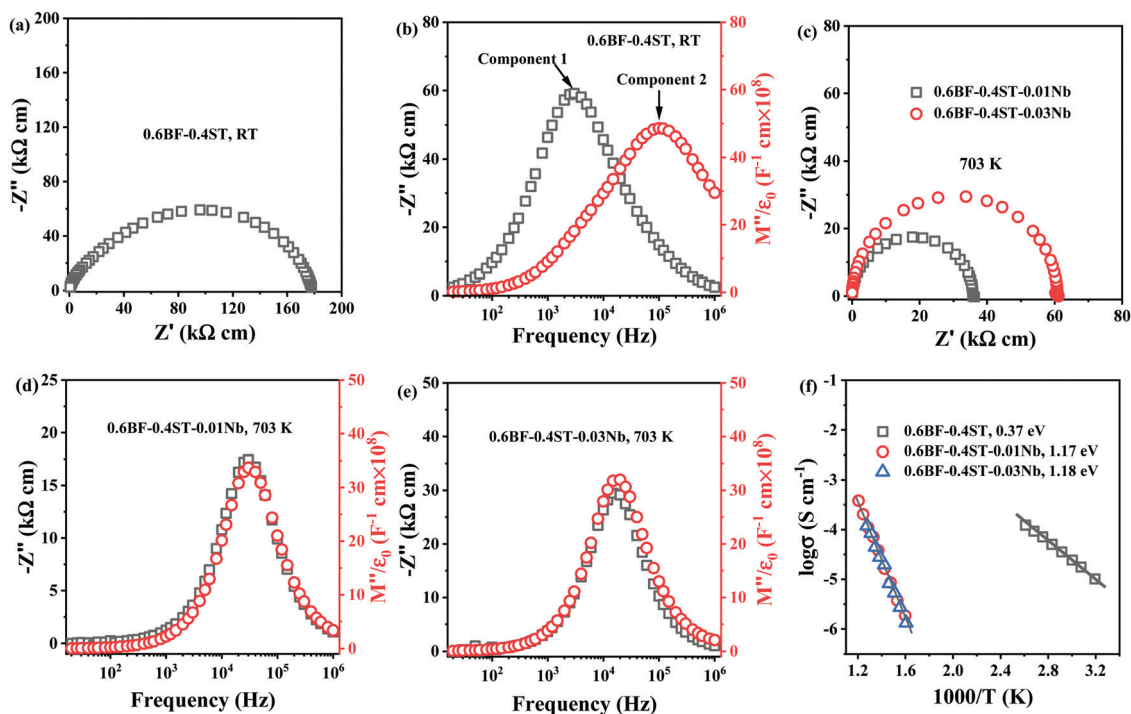


Fig. 1 (a)  $Z^*$  plots and (b)  $Z''$  and  $M''$  spectroscopic plots for 0.6BF–0.4ST ceramics at RT; (c)  $Z^*$  plots for 0.6BF–0.4ST–0.01Nb and 0.03Nb ceramics; (d) and (e)  $Z''$  and  $M''$  spectroscopic plots for 0.6BF–0.4ST–0.01Nb and 0.03Nb ceramics at 703 K, respectively; (f) Arrhenius plots of bulk conductivity extracted from  $M''$  spectra.



close to the intrinsic (band gap) mechanism and beneficial for BDS.<sup>49,50</sup> We conclude therefore, that p-type conduction mechanism has been successfully suppressed by Nb doping in BF-ST in accordance with eqn (3).

## 2.2. The role of sintering atmosphere on electrical conductivity

To establish the role of sintering atmosphere, preliminary studies were performed on 0.54–0.4ST–0.06BMN compositions without Nb doping (Section 2.3). Stoichiometric 5–6% BMN in BF–BaTiO<sub>3</sub> (BT), had been proved successful in promoting chemical homogeneity and increasing the resistivity in previous studies<sup>31,32</sup> and thus was considered a suitable initial concentration for investigation in this section.

Impedance data for 0.54BF–0.4ST–0.06BMN ceramics sintered in air and N<sub>2</sub> are shown in Fig. 2. Air sintered ceramics are leaky dielectrics at RT with a broadened and non-ideal arc in  $Z^*$  with a total resistivity of  $\sim 4$  M $\Omega$  cm, Fig. 2a. The  $Z''$  spectrum displays a single, resistive element (component 1),  $R_1 \sim 3.5$  M $\Omega$  cm and  $C_1 \sim 2.3 \times 10^{-10}$  F cm<sup>-1</sup> whereas the  $M''$  data shows the presence of a second element (component 2) that is more conductive,  $R_2 \sim 72$  k $\Omega$  cm and  $C_2 \sim 1.1 \times 10^{-10}$  F cm<sup>-1</sup> and evidence for a third (yet more conductive) element with a peak maximum  $> 1$  MHz, Fig. 2b. These ceramics are clearly electrically heterogeneous with resistive and conductive components. The  $M''$  spectrum for component 2 has a bulk-related  $C$  value and an Arrhenius plot of the conductivity ( $1/R_2$ ) for this component is given in Fig. 2c and shows an  $E_a$  of  $\sim 0.4$  eV. This is consistent with the p-type mechanism obtained for 0.6BF–0.4ST ceramics, Fig. 1f.

In contrast, ceramics sintered in N<sub>2</sub> are electrically insulating at RT and useful impedance data could only be obtained at  $> 573$  K. A  $Z^*$  plot for a sample measured at 613 K is shown in Fig. 2a and displays a single, near ideal arc with a total resistivity of  $\sim 0.16$  M $\Omega$  cm.  $Z''$ ,  $M''$  spectra (not shown) displayed a single Debye peak with a maximum at the same frequency with  $C \sim 1 \times 10^{-10}$  F cm<sup>-1</sup>, confirming a bulk-type response. Processing in N<sub>2</sub> dramatically improves the electrical homogeneity of the ceramics and suppresses the conductivity. An Arrhenius plot of the conductivity associated with the  $M''$

data is shown in Fig. 2c and displays much lower conductivity compared to air-fired ceramics with  $E_a \sim 0.86$  eV. Processing in N<sub>2</sub> therefore, suppresses p-type conductivity but 0.54BF–0.4ST–0.06BMN ceramics are  $\sim$ one order of magnitude more conductive than Nb-containing 0.6BF–0.4ST ceramics at  $\sim 623$  K ( $1000/T = 1.6$ ), Fig. 1f. This suggests that Nb-doping is more effective at suppressing p-type conductivity than processing in N<sub>2</sub>.

## 2.3. Nb doping in 0.54BF–0.4ST–0.06BMN–xNb (BF–ST–BMN–xNb) ceramics

X-ray diffraction (XRD) patterns of BF–ST–BMN–xNb ( $x = 0, 0.01, 0.02, 0.03, 0.04$  and  $0.05$ ) are shown in Fig. 3a. The ionic radii of Nb<sup>5+</sup> ions in 6-fold coordination is  $0.64$  Å and larger than the average for the B-site ions ( $0.625$  Å) (Ti<sup>4+</sup>,  $0.605$  Å and Fe<sup>3+</sup> high spin,  $0.645$  Å) for which it substitutes.<sup>51</sup> Thus, peaks shift to lower  $2\theta$  as the Nb content increases but for  $x > 0.03$ , the solid solubility is breached and additional secondary peaks are observed. Backscattered Electron (BSE) images of polished surfaces of the BF–ST–BMN–xNb ceramics are presented in Fig. S1 (ESI†) which present polygonal grains  $< 3$   $\mu$ m diameter with minimal porosity concomitant with relative density ( $\rho_r$ )  $> 95\%$ . Core-shell grains are observed in  $x = 0$  with most grains displaying bright, BF-rich cores and dark, ST-rich shells. The presence of the core-shell microstructure in some grains in the Nb doped ceramics is confirmed by transmission electron microscopy (TEM), as displayed in Fig. 3b and Fig. S2 (ESI†). Consistent with XRD patterns (Fig. 3a), secondary phases appear in the ceramics for  $x > 0.03$ . The detailed quantitative data for each microstructural feature observed in  $x = 0.05$  are listed in Table S1 (ESI†).

The appearance of a core-shell microstructure results from microchemical segregation, driven by immiscibility, into Bi, Fe and Sr, Ti rich regions during slow-cooling from sintering.<sup>31,32,37</sup> Although the microstructure arises from chemical heterogeneity, electrical homogeneity and low electrical conductivity have been demonstrated in previous studies through the use of dopants which modifies the defect chemistry of the core and shell such that they have similar resistivity based on impedance spectroscopy data.<sup>19</sup> The elimination of conducting cores through electrical homogeneity enhances BDS and facilitates the fabrication of

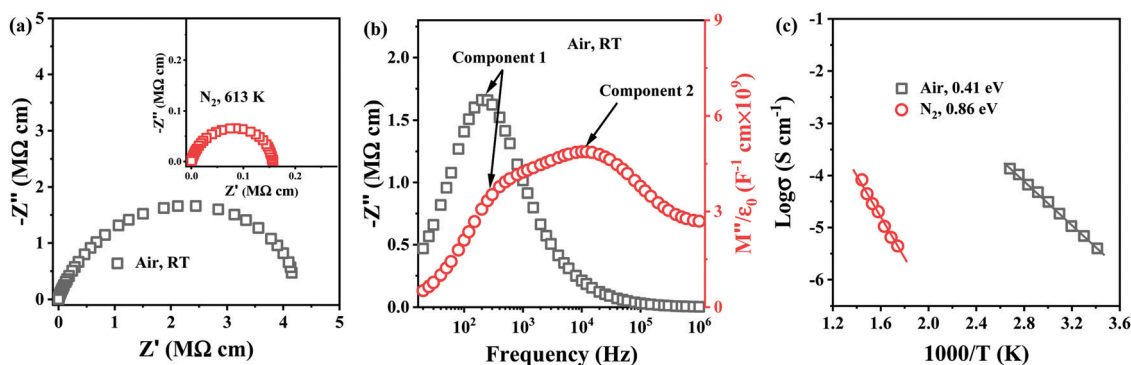


Fig. 2 (a)  $Z^*$  plots of the air sintered 0.54BF–0.4ST–0.06BMN ceramic at RT and the N<sub>2</sub> sintered ceramic at 613 K as inserted, respectively; (b)  $Z''$  and  $M''$  spectroscopic plots at RT of the ceramic sintered in air; (c) the Arrhenius plots of conductivity extracted from  $M''$  plots for ceramics sintered in air and N<sub>2</sub>.





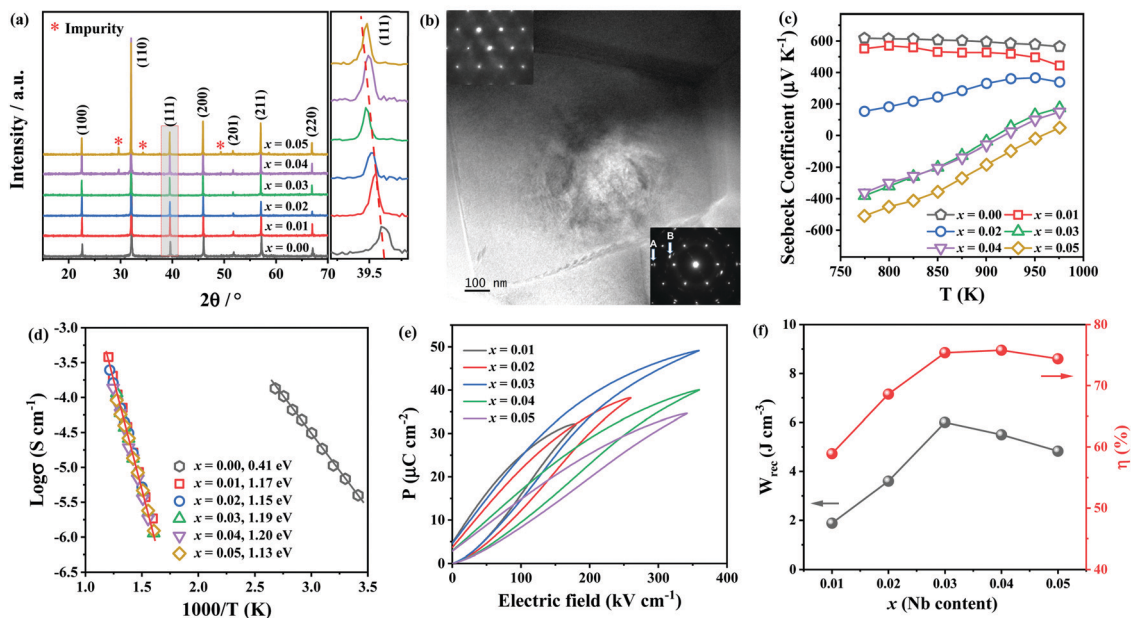
BF-ST-BMN-*x*Nb

Fig. 3 (a) XRD patterns, (b) TEM image obtained from  $x = 0.03$ , (c) Seebeck coefficients, (d) Arrhenius plots of conductivity obtained from  $M''$  peaks, (e) unipolar  $P$ – $E$  loops under  $E_{\max}$ , and (f) the energy storage properties,  $W_{\text{rec}}$  and  $\eta$  of BF-ST-BMN- $x$ Nb.

thinner dielectric layers suitable for MLCCs which do not short circuit under large applied field ( $> 500 \text{ kV cm}^{-1}$ ).<sup>19</sup>

The Seebeck coefficient ( $S$ ) of BF-ST-BMN- $x$ Nb ceramics as a function of temperature is shown in Fig. 3c. The positive  $S$  for  $x \leq 0.02$  indicates p-type conduction but the magnitude of  $S$  becomes smaller as  $x$  increases, presumably due to a decrease in  $n$ .<sup>52</sup> For  $x \geq 0.03$ ,  $S$  changes from positive to mixed negative and positive as a function of temperature, indicating a shift from p- to n-type conduction.<sup>53</sup> Typical  $Z^*$  plots and combined  $Z''$  and  $M''$  spectroscopic plots at 703 K of BF-ST-BMN- $x$ Nb ceramics are provided in Fig. S3a and b (ESI†). For  $x > 0$  compositions, only one semicircle is observed in the  $Z^*$  plot (Fig. S3a, ESI†), with a single Debye peak in both  $Z''$  and  $M''$  spectroscopic plots located at the same frequency (Fig. S3b, ESI†), indicating that all Nb doped ceramics are electrically homogeneous with only one parallel  $RC$  element.<sup>21</sup> The total electrical resistivity of the Nb doped ceramics is several orders of magnitude higher than undoped. The absence of a semicircle/peak in the impedance data between 12 and 273 K (Fig. S3c and d, ESI†) provides strong evidence that there are no high conductivity regions in the Nb doped samples. The incline in  $M''$  is not a conductive component but is due to relaxor-type behavior, as shown in Fig. S4 (ESI†). Nb Doping is therefore effective at suppressing the p-type conductivity and increasing the electrical homogeneity of BF-ST-BMN. The  $E_a$  increases from  $\sim 0.41 \text{ eV}$  for  $x = 0$  to  $\sim 1.20 \text{ eV}$  for  $x = 0.04$  and eventually drops to  $\sim 1.13 \text{ eV}$  for  $x = 0.05$  (Fig. 3d), indicating near intrinsic behaviour (band gap conduction) at  $x = 0.03$  and  $0.04$ , which is conducive to high BDS.<sup>49,50</sup>

The unipolar PE loops at maximum electric fields ( $E_{\max}$ ) of BF-ST-BMN- $x$ Nb ( $x = 0.01, 0.02, 0.03, 0.04, 0.05$ ) are shown in

Fig. 3e.  $x = 0$  is too conductive to be measured, however,  $E_{\max}$  is significantly enhanced for  $x > 0$  in agreement with impedance data (Fig. S3, ESI†). The calculated energy storage properties are plotted in Fig. 3f, with maximum  $W_{\text{rec}} = 6 \text{ J cm}^{-3}$  and  $\eta = 74.6\%$  at  $360 \text{ kV cm}^{-1}$  for  $x = 0.03$ .

#### 2.4. Variation of BMN with fixed Nb concentration (3%)

XRD patterns (Fig. 4a) reveal the unit cell volume of  $(0.6 - y)\text{BF} - 0.4\text{ST} - 0.03\text{Nb} - y\text{BMN}$  (BF-ST-Nb- $y$ BMN) expands (peaks shift to the lower  $2\theta$  angles) with increasing BMN content since the average ionic radii of  $\text{Mg}_{2/3}\text{Nb}_{1/3}$  in 6-fold coordination ( $0.693 \text{ \AA}$ ) is larger than  $\text{Fe}^{3+}$  (high spin,  $0.645 \text{ \AA}$ ).<sup>54</sup> BSE images acquired from BF-ST-Nb- $y$ BMN ( $y = 0.02, 0.04, 0.06, 0.08, 0.10$  and  $0.12$ ) ceramics are shown in Fig. S5 (ESI†). A core-shell microstructure is observed in all samples inside grains whose average grain size remains  $\sim 3 \mu\text{m}$ , irrespective of BMN concentration. For  $y = 0.10$  and  $0.12$ , Bi-rich secondary phases are observed.

$\epsilon_r$  and  $\tan \delta$  vs. temperature for BF-ST-Nb- $y$ BMN ceramics at  $100 \text{ kHz}$  (Fig. 4b) show all compositions exhibit a broad  $\epsilon_r$  maximum ( $\epsilon_{\text{max}}$ ) which is frequency dependent (Fig. S6, ESI†), consistent with relaxor behaviour.  $\epsilon_{\text{max}}$  decreases and broadens with increasing BMN concentration. The  $Z^*$  plots obtained from the ceramics at  $703 \text{ K}$  exhibit a single semicircle for each composition (Fig. S7a, ESI†) and co-incident Debye peaks in  $Z''$  and  $M''$  spectroscopic plots (Fig. S7b, ESI†). All data can be modelled on a single parallel  $RC$  element where bulk-type behavior dominates and therefore samples remain electrically homogeneous.<sup>21</sup> With increasing BMN concentration, ceramics become more resistive with a small increase in  $E_a$  (Fig. 4c), suggesting potential further enhancement in BDS.



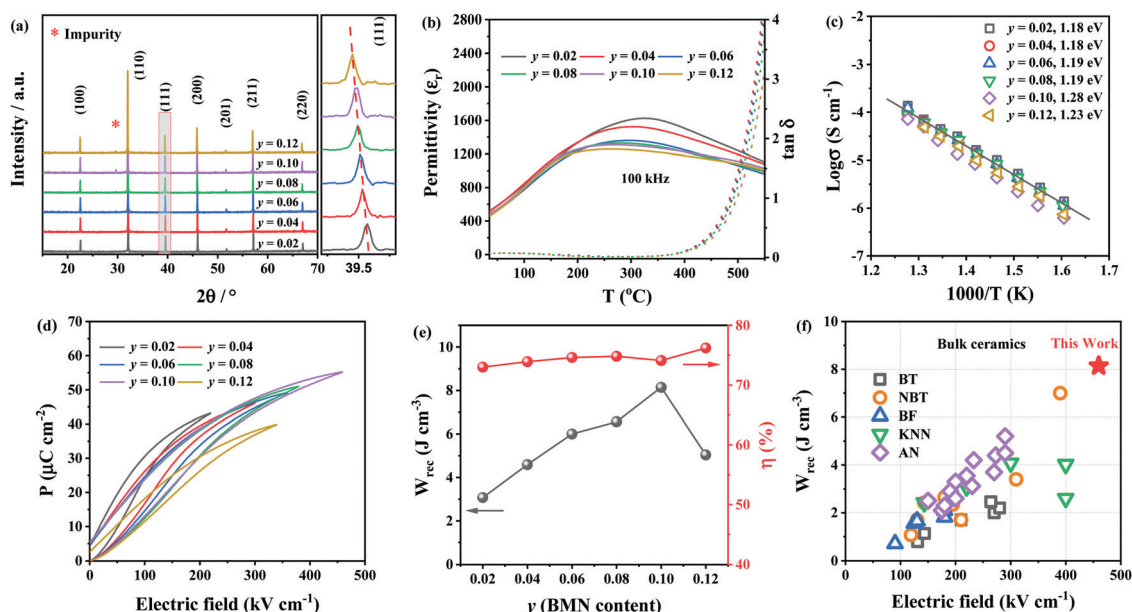
BF-ST-Nb-*y*BMN

Fig. 4 (a) The XRD patterns, (b) temperature dependent dielectric permittivity ( $\epsilon_r$  vs.  $T$ ) and loss ( $\tan \delta$  vs.  $T$ ) data at 100 kHz, (c) Arrhenius plots of conductivity obtained from  $M''$  peaks, (d) unipolar  $P$ - $E$  loops under  $E_{\max}$  and (e) energy storage properties,  $W_{\text{rec}}$  and  $\eta$  for BF-ST-Nb- $y$ BMN ( $y = 0.02, 0.04, 0.06, 0.08, 0.10$  and  $0.12$ ). (f) A comparison of  $W_{\text{rec}}$  for  $y = 0.10$  in this work with other lead-free bulk ceramics.<sup>11,12,55–59</sup>

$W_{\text{rec}}$  and  $\eta$  for BF-ST-Nb- $y$ BMN ( $y = 0.02, 0.04, 0.06, 0.08, 0.10$  and  $0.12$ ) ceramics extrapolated from unipolar  $P$ - $E$  loops under  $E_{\max}$  are shown in Fig. 4d and e. The substitution of BMN leads to slimmer and relaxor-like  $P$ - $E$  loops with higher  $\eta$  and higher BDS.  $W_{\text{rec}}$  reaches a maximum of  $8.2 \text{ J cm}^{-3}$  at  $460 \text{ kV cm}^{-1}$  with  $\eta$  of 74.1% for  $y = 0.10$ , which is the highest  $W_{\text{rec}}$  reported to date for lead-free bulk ceramics (see Fig. 4f).<sup>11,12,55–59</sup>

## 2.5. Landau-Devonshire (LD) phenomenological theory

The dopant strategies discussed in Sections 2.1–2.4 are not only designed to optimise the BDS but also to decrease the correlation length of polar coupling without decreasing the average ionic polarisability per unit volume. In this manner, it is proposed that  $P_{\max}$  may be optimised. However, this simplistic crystallochemical concept has to date not been proven in the context of a phenomenological model. Therefore, Landau-Devonshire (LD) phenomenological theory was employed to explore the microscopic origin of polarisation under  $E$  in BF-ST-Nb-BMN ceramics.<sup>90,91</sup>

A two-phase (rhombohedral and cubic, R + C) coexistence model is initially proposed in which the nano-polar regions (NPRs) with R structure are randomly nucleated and embedded in a C non-polar matrix, Fig. 5a. According to the local random field (LRF) model,<sup>92–95</sup> the polar regions are oriented along different polarisation directions, are isotropic and macroscopically paraelectric (with zero macroscopic polarisation), in agreement with a superparaelectric model.<sup>96</sup> The schematic picture of a three-dimensional (3D) Landau free-energy  $F(\vec{P})$  profile of polarisation rotation for BF-ST-Nb-BMN is given in Fig. 5b.  $F(\vec{P})$  of rhombohedral (R), tetragonal (T) and orthorhombic (O) phases

follows the sequence, R < T < O, indicating that R-phase is the only polar phase retained at RT at zero field. However, the energy barrier to polarisation rotation between  $\langle 111 \rangle_{\text{R}}$  and  $\langle 100 \rangle_{\text{T}}$  is small, as shown in the two-dimensional (2D) Landau free-energy curve, Fig. 5c, which suggests the polar phase may easily undergo polarisation rotation between  $\langle 111 \rangle$  and  $\langle 100 \rangle$  directions under an external  $E$ . The 2D  $F(\vec{P})$  curve of polarisation extension for BF-ST-Nb-BMN is shown in Fig. 5d, where a small energy barrier between the paraelectric (C) and ferroelectric (R) phases is found. With an external  $E$ , the  $F(\vec{P})$  of the relaxor is lowered, as shown in Fig. 5d, which indicates a large polarisation response is induced under a modest  $E$ . Consequently, the NPRs in BF-ST-Nb-BMN are easy to re-orientate and re-arrange in the direction of  $E$ , Fig. 5e, due to the small energy barriers associated with polarisation rotation and extension.<sup>97</sup>

According to the above, as  $E$  increases,  $P_{\max}$  for BF-ST-Nb-BMN is expected to keep increasing by both polarisation rotation and extension due to the small values of  $F(\vec{P})$ . As a result, provided a high BDS is maintained, a continuous increase of  $P$  with  $E$  is predicted leading to high  $W_{\text{rec}}$  and large  $\eta$ .

## 2.6. Multilayer ceramic capacitors

Sections 2.1–2.3 have systematically demonstrated how the resistivity and electrical homogeneity can be increased through Nb doping. Moreover, substituting BMN for BF (Section 2.4) in the formulation further disrupts long range polar order by introducing a wider spread of ion size and charge on the B-site without decreasing the average ionic polarisability of the solid solution. This has been shown by LD theory to maximise  $P$  in the direction of the applied field through polarisation



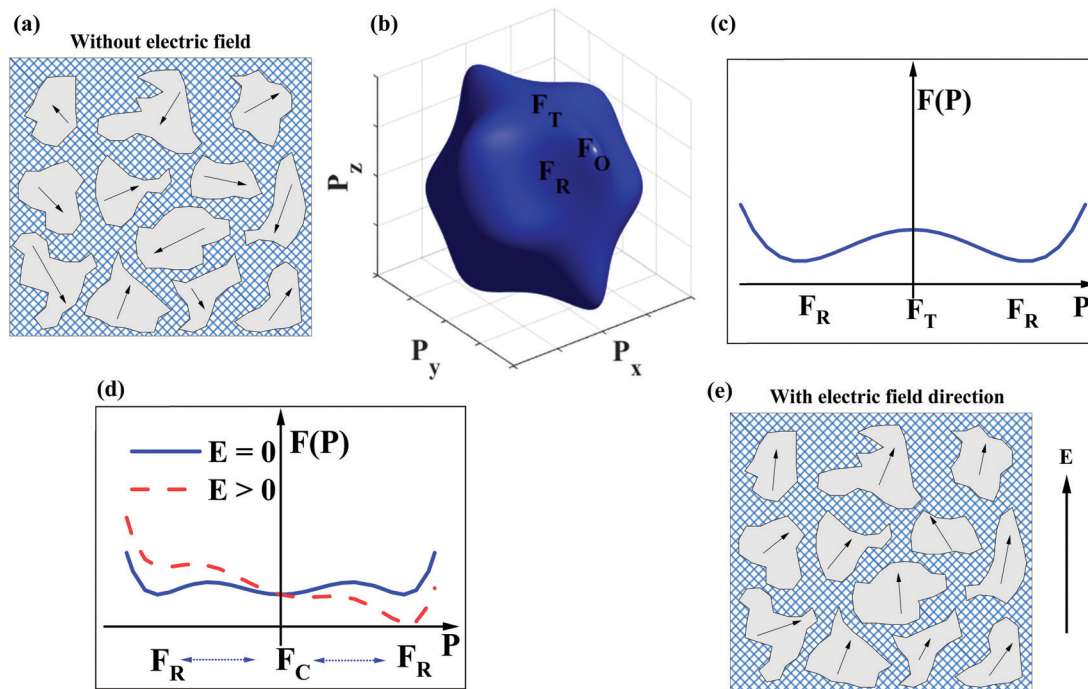


Fig. 5 (a) 2D cartoon of polar (R) coexisting with a non-polar cubic (C) phase without an external  $E$ . (b) 3D Landau free-energy profile of polarisation rotation for different polarisations under the two-phase (R + C) coexistence condition. (c) 2D Landau free-energy curve between  $\langle 111 \rangle_R$  and  $\langle 100 \rangle_T$  polarisation directions. (d) 2D Landau free-energy curve of polarisation extension  $F(P)$  under the two-phase (R + C) coexistence conditions with and without an external  $E$ . (e) 2D cartoon for the NPRs with an external  $E$  in a given direction.

extension and rotation (Section 2.5). In combination, these two effects have resulted in a highly resistive, electrically homogeneous, slim-looped relaxor with the potential of sustaining a high  $P_{\max}$  at high  $E$  without breakdown. In this section, we utilise a ceramic composition with the optimum  $W_{\text{rec}}$ , BF-ST-Nb-0.1BMN, and increase its BDS and thus  $P_{\max}$  through reduction in dielectric layer thickness, following the Gerson-Marshall relationship.<sup>98</sup>

An SEM image and corresponding energy-dispersive spectroscopy (EDS) elemental maps acquired from a cross section of a multilayer are illustrated in Fig. S8 (ESI†). The thickness and active electrode area of one dielectric layer are  $\sim 8 \mu\text{m}$  (Fig. S8, ESI†) and  $5 \text{ mm}^2$ , respectively. The interface between the Pt electrode and BF-ST-Nb-0.1BMN ceramic is characterised using (scanning) transmission electron microscopy ((S)TEM) with images, electron diffraction patterns and associated EDS maps shown in Fig. 6(a–f). According to the selected area diffraction (SAD) patterns in Fig. 6b and c, the  $\{011\}$  atomic planes of the ceramic grain displayed in Fig. 6a are  $\sim 7^\circ$  off parallel to  $\text{Pt}_{\{011\}}$  which is considered as a nominally random arrangement. However, a coherent 10–20 nm intermediate layer is observed at the surface of Pt. We propose that  $\text{Bi}^{3+}$  in the BF-based ceramic is reduced by residual carbon from the binder at the Pt/dielectric interface and forms an alloy with the Pt.<sup>99</sup> The EDS maps in Fig. 6e confirm the presence of Bi in the intermediate layer. In addition, discrete Bi-Pt phases, marked by  $\alpha$  and  $\beta$  in Fig. 6d are observed, the former of which based on Fig. 6e and f, is indexed as  $\text{Bi}_2\text{Pt}$ .

The unipolar  $P$ - $E$  loops and energy storage properties for the BF-ST-Nb-0.1BMN multilayer are shown in Fig. 6g–i.

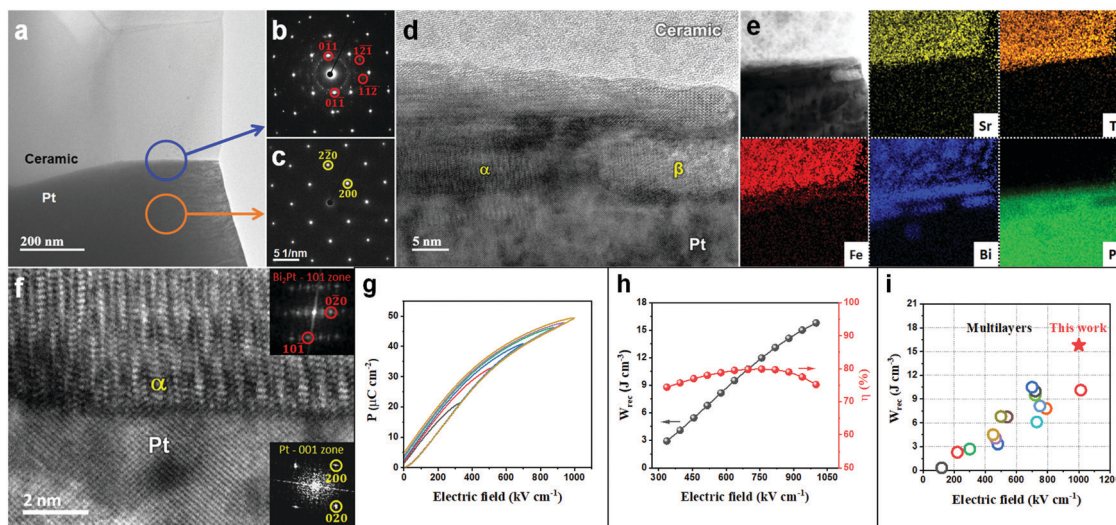
With increasing  $E$ ,  $W_{\text{rec}}$  increases until breakdown at  $> 1000 \text{ kV cm}^{-1}$ , thereby illustrating the enhancement in BDS in accordance with the Gerson-Marshall relationship.<sup>98</sup> The multilayer achieved the highest recorded  $W_{\text{rec}}$  of  $15.8 \text{ J cm}^{-3}$  with  $\eta = 75.2\%$  for random polycrystalline lead-free MLCCs. Given the high BDS, it is not clear how the formation of the Bi-Pt alloy affects the high field electrical properties but it is likely that reduction will locally affect  $P_{\max}$  in the vicinity of the interface by decreasing the concentration of the Bi-rich phase. Whether this also creates a local space charge layer, more conducting than the bulk of the dielectric within the multilayer, remains to be elucidated.

### 3. Conclusions

A systematic strategy to optimise BDS and  $P_{\max}$  in high energy density capacitors is presented. Nb doping increases resistivity by eliminating p-type leakage conduction and promotes electrical homogeneity whereas a third perovskite end-member, BMN, mainly promotes relaxor behaviour for which Landau-Devonshire theory predicts a large microscopic polarisation originating from its flat thermodynamic energy profile. This results in an increase in BDS and  $P_{\max}$  at high field to give  $W_{\text{rec}} = 8.2 \text{ J cm}^{-3}$  at  $460 \text{ kV cm}^{-1}$  for BF-ST-0.03Nb-0.1BMN ceramics which facilitated a multilayer with  $8 \mu\text{m}$  dielectric layer thickness with  $\text{BDS} > 1000 \text{ kV cm}^{-1}$  and  $W_{\text{rec}} = 15.8 \text{ J cm}^{-3}$ . The multilayer showed evidence of interfacial reactions and Bi-Pt alloy formation which might, despite the very high BDS, have been deleterious to  $W_{\text{rec}}$  by decreasing  $P_{\max}$ .







**Fig. 6** (a) TEM micrograph obtained from an interface between a BF-ST-Nb-0.1BMN grain and a Pt grain (electrode). Here the Pt grain is close to its [001] zone axis and the BF-ST-Nb-0.1BMN grain is  $\sim 10^\circ$  off from its [311] zone axis. (b) SAD pattern obtained from the area marked by a blue circle shown on (a) i.e. interface between BF-ST-Nb-0.1BMN and Pt. Here, few reflections related to BF-ST-Nb-0.1BMN are marked by red circles. (c) SAD pattern obtained from the area marked by an orange circle shown on (a), i.e. Pt. (d) High resolution TEM micrograph obtained from the interface between ceramic and Pt shown in (a). Here different phases (e.g.  $\alpha$  and  $\beta$ ) are observed at the surface of Pt. (e) A bright-field STEM image and corresponding chemical EDS elemental maps obtained from the interface between ceramic and Pt shown in (a). (f) A bright-field STEM image obtained from the interface between Pt and  $\alpha$  shown in (d). (g) Unipolar  $P$ - $E$  loops. (h) The energy storage properties,  $W_{\text{rec}}$  and  $\eta$ , for BF-ST-Nb-0.1BMN multilayer. (i) A comparison for  $W_{\text{rec}}$  of the multilayer in this work with other lead-free multilayers reported in ref. 10, 12, 13, 21, 56 and 100–109.

## 4. Experimental

BF-ST based systems,  $0.6\text{BiFeO}_3\text{-}0.4\text{SrTiO}_3\text{-}x\text{Nb}$  ( $x = 0, 0.01, 0.03$ ),  $0.54\text{BiFeO}_3\text{-}0.4\text{SrTiO}_3\text{-}0.06\text{Bi}(\text{Mg}_{2/3}\text{Nb}_{1/3})\text{O}_3\text{-}x\text{Nb}$  (BF-ST-BMN- $x\text{Nb}$ ,  $x = 0, 0.01, 0.02, 0.03, 0.04$  and  $0.05$ ) and  $(0.6 - y)\text{BiFeO}_3\text{-}0.4\text{SrTiO}_3\text{-}0.03\text{Nb-yBi}(\text{Mg}_{2/3}\text{Nb}_{1/3})\text{O}_3$ , (BF-ST-Nb- $y\text{BMN}$ ,  $y = 0.02, 0.04, 0.06, 0.08, 0.10$  and  $0.12$ ) ceramics were synthesised using analytical-grade raw chemicals of  $\text{Bi}_2\text{O}_3$ ,  $\text{Fe}_2\text{O}_3$ ,  $\text{SrCO}_3$ ,  $\text{TiO}_2$ ,  $\text{MgO}$  and  $\text{Nb}_2\text{O}_5$  by a conventional solid state reaction method. Stoichiometric amounts of dry raw powders were weighed, and ball milled for 6 hours with  $\text{Y}_2\text{O}_3$ -stabilized  $\text{ZrO}_2$  grinding media in isopropanol. The mixed powders were calcined at  $800^\circ\text{C}$  for 2 hours and then ball milled again for 6 hours prior to sintering. The final dry powders were uniaxially pressed into 8 mm diameter pellets then sintered at  $1070\text{--}1100^\circ\text{C}$  for 3 hours in air or  $\text{N}_2$ . The same dry powder was used to fabricate ceramic multilayers using an MTI MSK-AFA-II tape caster.<sup>21</sup> A DEK 247 screen printer was employed to print Pt electrodes onto the tape, followed by stacking and hot-pressing at  $80^\circ\text{C}$  for 20 min. Multilayers were sintered using the same procedure as for the bulk ceramics but with the addition of two more intermediate binder burnout steps ( $180^\circ\text{C}$  for 3 h and  $300^\circ\text{C}$  for 3 h).

X-ray diffraction (XRD) on ceramics was performed using a Bruker D2 phaser. The operating voltage and current were 40 kV and 30 mA, respectively. The polished surface morphology of ceramic samples was examined using a FEI Inspect F50 scanning electron microscope (SEM) with BSE and EDS detectors. Samples for (scanning) transmission electron microscopy ((S)TEM) were mechanically grounded to reach a thickness of  $\sim 50\ \mu\text{m}$ . Further polishing was conducted at liquid nitrogen temperature by  $\text{Ar}^+$  ion milling using a Gatan Precision Ion Polishing System PIPS (II).

(S)TEM data were acquired with a JEOL JEM 2100F (JEOL, Tokyo, Japan) operated at 200 kV. Impedance spectroscopy (IS) data were collected using an Agilent E4980A (Agilent Technologies Inc., Palo-Alto, CA) from 20 Hz–2 MHz and from 12 to 873 K with an ac voltage of 100 mV. Resistivity of samples was obtained by fitting the experimental IS data using ZView software (Scribner Associates, Inc., Southern Pines, NC). The temperature dependence of the dielectric properties (permittivity and  $\tan\delta$ ) were measured using an Agilent 4184A precision LCR meter from room temperature (RT) to  $550^\circ\text{C}$  at 1, 10, 100, 250 kHz and 1 MHz. IS and LCR data were corrected by a geometric factor (thickness/surface area). For ferroelectric polarisation-field ( $P$ - $E$ ) loops measurements, ceramics were ground to a thickness of  $\sim 0.15\ \text{mm}$  and then gold sputtered. Bipolar  $P$ - $E$  loops were obtained using an aixACCT TF 2000E ferroelectric tester at 1 Hz.

## Conflicts of interest

There are no conflicts of interest to declare.

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Piezoelectric Transformer power supplies, FPeT' (EP/P015859/1) and support provided by the Functional Materials and Devices group at The University of Sheffield.

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